

Noncentrosymmetric Polar Oxide Material,  $\text{Pb}_3\text{SeO}_5$ : Synthesis, Characterization, Electronic Structure Calculations, and Structure–Property Relationships

Sang-Hwan Kim, Jeongho Yeon, and P. Shiv Halasyamani\*

Department of Chemistry, University of Houston, 136 Fleming Building, Houston, Texas 77204-5003

Received August 26, 2009. Revised Manuscript Received September 29, 2009

A noncentrosymmetric (NCS) polar compound,  $\text{Pb}_3\text{SeO}_5$ , has been hydrothermally synthesized and structurally characterized by single crystal X-ray diffraction.  $\text{Pb}_3\text{SeO}_5$  exhibits a two-dimensional crystal structure consisting of layers of  $\alpha\text{-PbO}$ -like “slabs” that are linked through  $\text{SeO}_3$  polyhedra. Structurally, it is the bridging  $\text{SeO}_3$  polyhedra between the  $\alpha\text{-PbO}$ -like slabs that results in the NCS and polar nature of  $\text{Pb}_3\text{SeO}_5$ . Powder second-harmonic generation (SHG) measurements using 1064 nm radiation indicates that  $\text{Pb}_3\text{SeO}_5$  exhibits a strong SHG efficiency of  $\sim 300 \times \alpha\text{-SiO}_2$ . Additional SHG measurements indicate the material is type-I phase-matchable. Converse piezoelectric measurements revealed a  $d_{33}$  value of  $\sim 81$  pm/V, and a pyroelectric coefficient of  $-42 \mu\text{C}/(\text{m}^2 \text{K})$  at  $65^\circ\text{C}$  was also determined. Using first principle density functional theory (DFT) calculations, we demonstrated that polarization reversal in  $\text{Pb}_3\text{SeO}_5$  is not energetically favorable—the material is polar but *not* ferroelectric. Our calculations also indicate that both  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$  cations exhibit a stereoactive lone-pair. In addition, differential scanning calorimetry measurements revealed an irreversible phase transition at  $\sim 440^\circ\text{C}$ . Finally, infrared, UV–vis and thermogravimetric measurements were also performed. Crystal data:  $\text{Pb}_3\text{SeO}_5$ , orthorhombic, space group  $\text{Cmc}2_1$  (no. 36),  $a = 10.5211(13)$  Å,  $b = 10.7151(13)$  Å,  $c = 5.7452(7)$  Å,  $V = 647.68(14)$  Å<sup>3</sup>, and  $Z = 2$ .

## Introduction

Understanding the origin of asymmetry in noncentrosymmetric (NCS) solid-state materials<sup>1</sup> is critically important as it would enable us to design new materials exhibiting technologically relevant physical properties such as ferroelectricity and pyroelectricity.<sup>2–5</sup> These properties are directly related to macroscopic polarization changes and are intimately correlated to the NCS crystal classes.<sup>6,7</sup> In order to exhibit ferroelectricity or pyroelectricity, all materials must crystallize in one of ten polar crystal classes, 1, 2, 3, 4, 6, *m*, *mm*2, *3m*, *4mm*, or *6mm*.<sup>8</sup> Common asymmetric building units in NCS oxide materials include distorted  $\text{MO}_6$  octahedra ( $\text{M} = \text{d}^0$

transition metal cation:  $\text{Ti}^{4+}$ ,  $\text{Nb}^{5+}$ ,  $\text{W}^{6+}$ , etc.)<sup>9–14</sup> as well as asymmetric  $\text{AO}_x\text{E}$  polyhedra ( $A = \text{lone-pair cation: Se}^{4+}$ ,  $\text{I}^{5+}$ ,  $\text{Pb}^{2+}$ , etc. and  $E = \text{lone-pair}$ ).<sup>15–28</sup> Microscopically, these polyhedra exhibit dipole moments that when aligned result in a macroscopically polar NCS material. With respect to the  $\text{MO}_6$  and  $\text{AO}_x\text{E}$  polyhedra, second-order Jahn–Teller (SOJT) effects have been invoked to explain the local polar coordination environments of the  $\text{d}^0$  transition metal

- (1) Preiser, C.; Losel, J.; Brown, I. D.; Kunz, M.; Skowron, A. *Acta Crystallogr., Sect. B* **1999**, *B55*, 698.
- (2) Auciello, O.; Scott, J. F.; Ramesh, R. *Phys. Today* **1998**, *51*, 22.
- (3) Haertling, G. H. *J. Am. Ceram. Soc.* **1999**, *82*, 797.
- (4) Lang, S. B.; Das-Gupta, D. K. Pyroelectricity: Fundamentals and Applications. In *Handbook of Advanced Electronic and Photonic Materials and Devices*; Nalwa, H. S., Ed.; Academic Press: San Francisco, 2001; Vol. 4, pp 1–55.
- (5) Lang, S. B. *Phys. Today* **2005**, *58*, 31.
- (6) Nye, J. F. *Physical Properties of Crystals*; Oxford University Press: Oxford, 1957.
- (7) Halasyamani, P. S.; Poeppelmeier, K. R. *Chem. Mater.* **1998**, *10*, 2753.
- (8) Hahn, T. *International Tables for Crystallography, Volume A, Space Group Symmetry*; Kluwer Academic: Dordrecht, Holland, 2006; Vol. A.
- (9) Abrahams, S. C.; Hamilton, W. C.; Reddy, J. M. *J. Phys. Chem. Solids* **1966**, *27*, 1013.
- (10) Jamieson, P. B.; Abrahams, S. C. *Acta Crystallogr., Sect. B* **1968**, *24*, 984.

- (11) Jamieson, P. B.; Abrahams, S. C.; Bernstein, J. L. *J. Chem. Phys.* **1969**, *50*, 4352.
- (12) Goodenough, J. B. *Annu. Rev. Mater. Sci.* **1998**, *28*, 1.
- (13) Halasyamani, P. S. *Chem. Mater.* **2004**, *16*, 3586.
- (14) Sun, C.-F.; Hu, C.-L.; Xu, X.; Ling, J.-B.; Hu, T.; Kong, F.; Long, X.-F.; Mao, J.-G. *J. Am. Chem. Soc.* **2009**, *131*, 9486.
- (15) Bergman, J. G.; Crane, G. R. *J. Solid State Chem.* **1975**, *12*, 172.
- (16) Galy, J.; Meunier, G.; Andersson, S.; Astrom, A. *J. Solid State Chem.* **1975**, *13*, 142.
- (17) Raveau, B. *Rev. Silicon, Germanium, Tin Lead Compd.* **1982**, *6*, 287.
- (18) Serezhkin, V. N.; Buslaev, Y. A. *Zh. Neorg. Khim.* **1997**, *42*, 1180.
- (19) Serezhkin, V. N.; Serezhkin, L. B.; Furmanova, N. G.; Buslaev, Y. A. *Zh. Neorg. Khim.* **1997**, *42*, 1879.
- (20) Porter, Y.; Ok, K. M.; Bhuvanesh, N. S. P.; Halasyamani, P. S. *Chem. Mater.* **2001**, *13*, 1910.
- (21) Ok, K. M.; Bhuvanesh, N. S. P.; Halasyamani, P. S. *Inorg. Chem.* **2001**, *40*, 1978.
- (22) Ok, K. M.; Halasyamani, P. S. *Inorg. Chem.* **2005**, *44*, 2263.
- (23) Kong, F.; Huang, S.-P.; Sun, Z.-M.; Mao, J.-G.; Cheng, W.-D. *J. Am. Chem. Soc.* **2006**, *128*, 7750.
- (24) Barrier, N.; Malo, S.; Hernandez, O.; Hervieu, M.; Raveau, B. *J. Solid State Chem.* **2006**, *179*, 3484.
- (25) Mayerova, Z.; Johnsson, M.; Lidin, S. *Angew. Chem., Int. Ed.* **2006**, *45*, 5602.
- (26) Rieger, F.; Mudring, A.-V. *Inorg. Chem.* **2007**, *46*, 446.
- (27) Mao, J.-G.; Jiang, H.-L.; Kong, F. *Inorg. Chem.* **2008**, *47*, 8498.
- (28) Chang, H.-Y.; Kim, S.-H.; Ok, K. M.; Halasyamani, P. S. *J. Am. Chem. Soc.* **2009**, *131*, 6865.

and lone-pair cation.<sup>12,29–34</sup> Deeper insight with respect to lone-pair formation in heavier p-metal cations such as  $\text{TI}^+$ ,  $\text{Pb}^{2+}$ , and  $\text{Bi}^{3+}$  has been reported experimentally.<sup>35</sup> Theoretical examinations of their electronic structures through comparing hypothetical symmetric and experimental NCS crystal structures revealed that the stereoactive lone-pair formation is primarily driven by the interactions between the s- and p-orbitals in the metal cation and oxide anions, respectively, and not solely by intra-atomic sp-orbital mixing of the cations.<sup>36–39</sup> The interactions are thought to be mediated through cation or anion p-orbitals in low-lying unoccupied states. Despite the great success regarding the elucidation of the local asymmetry, the reasons why the asymmetric polyhedra sometimes align in solid-state structures is often unclear.

With extended solid-state materials such as  $\text{ANa-NbOF}_5$  ( $\text{A} = \text{K}^+$  or  $\text{Cs}^+$ ), Poeppelmeier et al. have reported that different cation–anion interactions in the bond network result in NCS polar and centrosymmetric non-polar structures.<sup>40</sup> We recently reported that the  $\text{A}^+$  cation in  $\text{A}_2\text{Ti}(\text{IO}_3)_6$  ( $\text{A} = \text{Li}^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$ ,  $\text{Cs}^+$ , or  $\text{TI}^+$ ) is a dominant factor in the material's macroscopic polarity.<sup>41</sup> Materials in the  $\text{PbO-SeO}_2$  system are of interest attributable to the occurrence of lone-pairs on  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$ . Ternary oxides in this system include  $\text{PbSeO}_3$ ,  $\text{PbSe}_2\text{O}_5$ ,  $\text{Pb}_3\text{SeO}_5$ , and  $\text{Pb}_5\text{SeO}_7$ ,<sup>42–45</sup> and of these, only  $\text{Pb}_3\text{SeO}_5$  is NCS and polar. No functional properties with respect to the polarity of  $\text{Pb}_3\text{SeO}_5$  have been reported. In this paper, we not only report on the synthesis and structure of  $\text{Pb}_3\text{SeO}_5$ , but we also investigate the material's functional properties—second-harmonic generation, piezoelectricity, ferroelectricity, and pyroelectricity. In addition, electronic structure calculations have been performed to examine the local polarity associated with  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$ , i.e., their lone-pair, as well as the macroscopic polarity observed in  $\text{Pb}_3\text{SeO}_5$ . Our calculations indicate that the local polarity in  $\text{Pb}_3\text{SeO}_5$  is energetically very unfavorable toward reversibility—the material is pyroelectric and *not* ferroelectric. From the

Table 1. Crystallographic Data for  $\text{Pb}_3\text{SeO}_5$ 

formula	$\text{Pb}_3\text{SeO}_5$
fw (g/mol)	780.53
$T$ (K)	296.0(2)
$\lambda$ (Å)	0.71073
crystal system	orthorhombic
space group	$\text{Cmc}2_1$ (no. 36)
$a$ (Å)	10.5211(13)
$b$ (Å)	10.7151(13)
$c$ (Å)	5.7452(7)
$V$ (Å <sup>3</sup> )	647.68(14)
$Z$	4
$\rho_{\text{calcd}}$ (g/cm <sup>3</sup> )	8.007
$\mu$ (mm <sup>−1</sup> )	83.357
$2\theta_{\text{max}}$ (deg)	57.4
$R(\text{int})$	0.0687
$\text{GOF}(F^2)$	1.031
$R(F)^a$	0.0301
$R_w(F_o^2)^b$	0.0509
Flack param	0.04(2)

$$^a R(F) = \sum ||F_o| - |F_c|| / \sum |F_o|, \quad ^b R_w(F_o^2) = [\sum w(F_o^2 - F_c^2)^2 / \sum w(F_o^2)^2]^{1/2}.$$

direct space analyses, stereoactive lone-pairs are observed near all the cations. We also examined the thermal properties and observed an irreversible phase transition at around 440 °C. This transition is unexpected since it has been reported that  $\text{Pb}_3\text{SeO}_5$  is stable from 470 to 610 °C and is formed through the thermal dissociation of  $\text{PbSeO}_3$ .<sup>42</sup> In this paper, we report on the synthesis, structure, functional properties, and electronic structure characterization, as well as infrared, thermogravimetric, and differential scanning calorimetry measurements of  $\text{Pb}_3\text{SeO}_5$ .

## Experimental Section

**Reagents.**  $\text{PbO}$  (Aldrich, 99.9%),  $\text{SeO}_2$  (Alfa Aesar, 99%), and  $\text{NaOH}$  (Aldrich, 99%) were used as received.

**Synthesis.**  $\text{Pb}_3\text{SeO}_5$  was hydrothermally synthesized by combining 1.00 g (4.50 mmol) of  $\text{PbO}$  and 0.50 g (4.50 mmol) of  $\text{SeO}_2$  with 8 mL of 1 M  $\text{NaOH}(\text{aq})$ . The mixture was placed in a 23-mL Teflon-lined autoclave that was subsequently sealed. The autoclave was gradually heated to 230 °C, held for 2 days, and cooled slowly to room temperature at a rate 6 °C/h. The mother liquor was decanted, and the product, transparent colorless rod-shaped crystals, was recovered by filtration and washed with excess amounts of distilled water and acetone. The colorless rod-shaped crystals were obtained in nearly quantitative yield.

**Single Crystal X-ray Diffraction.** A colorless rod-shaped crystal ( $0.02 \times 0.02 \times 0.08 \text{ mm}^3$ ) was chosen for single-crystal X-ray collection. The data were collected using a Siemens SMART APEX diffractometer equipped with a 1 K CCD area detector using graphite-monochromated  $\text{Mo K}\alpha$  radiation. A hemisphere of data was collected using a narrow-frame method with scan widths of  $0.30^\circ$  in  $\omega$ , and an exposure time of 60s per frame. The data were integrated using the Siemens SAINT program,<sup>46</sup> with the intensities corrected for Lorentz-Polarization, air absorption, and absorption attributable to the variation in the path length through the detector face plate. Psi-scans were used for the absorption correction on the data.

- (29) Opik, U.; Pryce, M. H. L. *Proc. R. Soc. London, Ser. A* **1957**, 238, 425.
- (30) Bader, R. F. W. *Mol. Phys.* **1960**, 3, 137.
- (31) Bader, R. F. W. *Can. J. Chem.* **1962**, 40, 1164.
- (32) Pearson, R. G. *J. Mol. Struct.: THEOCHEM* **1983**, 103, 25.
- (33) Pearson, R. G. *J. Am. Chem. Soc.* **1969**, 91, 4947.
- (34) Wheeler, R. A.; Whangbo, M. H.; Hughbanks, T.; Hoffmann, R.; Burdett, J. K.; Albright, T. A. *J. Am. Chem. Soc.* **1986**, 108, 2222.
- (35) Payne, D. J.; Egdel, R. G.; Walsh, A.; Watson, G. W.; Guo, J.; Glans, P. A.; Learmonth, T.; Smith, K. E. *Phys. Rev. Lett.* **2006**, 96, 157403/1.
- (36) Watson, G. W.; Parker, S. C. *J. Phys. Chem. B* **1999**, 103, 1258.
- (37) Seshadri, R.; Hill, N. A. *Chem. Mater.* **2001**, 13, 2892.
- (38) Mudring, A.-V.; Rieger, F. *Inorg. Chem.* **2005**, 44, 6240.
- (39) Stoltzfus, M. W.; Woodward, P.; Seshadri, R.; Park, J.-H.; Bursten, B. *Inorg. Chem.* **2007**, 46, 3839.
- (40) Marvel, M. R.; Lesage, J.; Baek, J.; Halasyamani, P. S.; Stern, C. L.; Poeppelmeier, K. R. *J. Am. Chem. Soc.* **2007**, 2007, 13963.
- (41) Chang, H. Y.; Kim, S.-H.; Ok, K. M.; Halasyamani, P. S. *Chem. Mater.* **2009**, 21, 1654.
- (42) Lahtinen, M.; Valkonen, J. *Chem. Mater.* **2002**, 14, 1812.
- (43) Zlomanzov, V. P.; Popovkin, B. A.; Tananaeva, O. I.; Novoselova, A. V. *Zh. Neorg. Khim.* **1962**, 7, 2746.
- (44) Popovkin, B. A.; Novoselova, A. V. *Dokl. Akad. Nauk SSSR* **1961**, 139, 117.
- (45) Krivovichev, S. V.; Avdontseva, E. Y.; Burns, P. C. *Z. Anorg. Allg. Chem.* **2004**, 630, 558.

- (46) SAINT Program for Area Detector Absorption Correction, 4.05; Siemens Analytical X-ray Systems, Inc.: Madison, WI, 1995.
- (47) Sheldrick, G. M. *SHELXTL DOS/Windows/NT, 5.10*; Bruker Analytical X-Ray Instruments, Inc.: Madison, WI, 1997.
- (48) Sheldrick, G. M. *SHELXS-97 - A program for automatic solution of crystal structures*; University of Goettingen: Goettingen, Germany, 1997.

**Table 2. Atomic Coordinates and Equivalent Isotropic Displacement Parameters (Å) for Pb<sub>3</sub>SeO<sub>5</sub>**

	<i>x</i>	<i>y</i>	<i>z</i>	<i>U</i> <sub>eq</sub> <sup>a</sup>
Pb(1)	0.0000	0.38218(4)	0.9461(3)	0.01257(19)
Pb(2)	−0.24759(3)	0.61215(3)	0.95133(10)	0.01469(15)
Se	0.0000	0.12986(12)	0.3990(3)	0.0106(4)
O(1)	−0.1345(4)	0.4957(10)	0.715(2)	0.0133(12)
O(2)	0.0000	0.2788(7)	0.491(2)	0.022(2)
O(3)	0.1284(6)	0.0708(6)	0.5417(10)	0.0193(15)

<sup>a</sup> *U*<sub>eq</sub> is defined as one-third of the trace of the orthogonalized *U*<sub>ij</sub> tensor.

**Table 3. Selected Bond Distances (Å) in Pb<sub>3</sub>SeO<sub>5</sub>**

Pb(1)–O(1) × 2	2.291(9)	Pb(2)–O(1)	2.195(10)
Pb(1)–O(1) × 2	2.470(10)	Pb(2)–O(1)	2.246(10)
		Pb(2)–O(3)	2.411(6)
		Pb(2)–O(3)	2.727(6)
Se–O(2)	1.681(9)		
Se–O(3) × 2	1.703(6)		

The data were solved by direct and refined against *F*<sup>2</sup> by full-matrix least-squares techniques using SHELXS-97 and SHELXL-97, respectively.<sup>47–49</sup> All of the atoms in the structure were refined with anisotropic thermal parameters, and the refinements converged for *I* > 2σ(*I*). The Flack parameter was refined to 0.04(2). The structure was checked for missing symmetry elements using PLATON.<sup>50</sup> Relevant crystallographic data, atomic coordinates and thermal parameters, and selected bond distances for Pb<sub>3</sub>SeO<sub>5</sub> are given in Tables 1, 2, and 3, respectively.

**Powder X-ray Diffraction.** Powder X-ray diffraction (PXRD) data were collected using a PANalytical X'Pert PRO diffractometer using Cu Kα radiation. The 2θ range was 5–90° with a step size of 0.0167° and a fixed time of 0.2s. The PXRD pattern is in good agreement with the calculated PXRD from the single crystal model (see Figure S1 of the Supporting Information). From the thermogravimetric and differential scanning calorimetric studies (see below), we observed a phase transition at ~440 °C.

**Thermogravimetric Analysis.** Thermogravimetric analysis was carried out on a TGA 951 thermogravimetric analyzer (TA Instruments). The sample was placed in a platinum crucible and heated at a rate of 10 °C min<sup>−1</sup> from room temperature to 900 °C under flowing nitrogen. The TGA data has been deposited in the Supporting Information (see Figure S2).

**Differential Scanning Calorimetry Analysis.** Differential scanning calorimetry (DSC) analysis was performed on an EXSTAR6000 Differential Scanning Calorimeter (SII Nano-Technology Inc.). A 10.0 mg portion of the sample was placed in an aluminum pan covered by an aluminum lid that was heated (cooled) at a rate of 10 °C min<sup>−1</sup> between 25 and 500 °C under flowing air. Alumina was used as the reference during the measurements.

**Infrared Spectroscopy.** Infrared spectra were recorded on a Matteson FTIR 5000 spectrometer in the 400–3000 cm<sup>−1</sup> range (see Figure S3 in the Supporting Information). The IR spectra revealed Pb–O (Se–O) vibrations at 457 cm<sup>−1</sup> (435, 515, 726, and 790 cm<sup>−1</sup>) consistent with published reports.<sup>51–53</sup>

**UV–vis Diffuse Reflectance Spectroscopy.** UV–visible reflectance data were collected on a Varian Cary 500 scan UV–vis–NIR spectrophotometer over the 200–1500 nm spectral range at room temperature. Poly(tetrafluoroethylene) was used as a reference material. The reflectance spectrum was converted to absorbance using the Kubelka–Munk function (see Figure S4 in the Supporting Information).<sup>54,55</sup>

**Second Harmonic Generation (SHG).** Powder SHG measurements were performed on a modified Kurtz–NLO<sup>56</sup> system using a pulsed Nd:YAG laser with a wavelength of 1064 nm. A detailed description of the equipment and methodology has been published.<sup>57</sup> The SHG efficiency has been shown to depend strongly upon particle size,<sup>56</sup> thus polycrystalline samples were ground and sieved into distinct particle size ranges (20–45, 45–63, 63–75, 75–90, > 90 μm). In order to make relevant comparisons with known SHG materials, crystalline α-SiO<sub>2</sub> and LiNbO<sub>3</sub> were also ground and sieved into the same particle size ranges. No index matching fluid was used in any of the experiments.

**Piezoelectric Measurements.** Converse piezoelectric measurements were performed using a Radiant Technologies RT66A piezoelectric test system with a TREK (model 609 × 10<sup>−6</sup>) high-voltage amplifier, Precision Materials Analyzer, Precision High-Voltage Interface, and MTI 2000 Fotonic Sensor. Pb<sub>3</sub>SeO<sub>5</sub> was pressed into 12-mm diameter, ~1-mm-thick pellets using a cold isostatic press at 3500 psi at room temperature, after which the material was heated to 300 °C for 7 days. Initially silver paste was applied on both sides of the pellet. Upon curing at 200 °C, gold was deposited on both sides of a fresh pellet with silver applied on top of the gold. This pellet was cured at 200 °C for 3 h. Solely using gold was not possible attributable to the poor optical sensitivity in measuring the converse piezoelectricity. A maximum voltage of 30 kV/cm was applied to the sample.

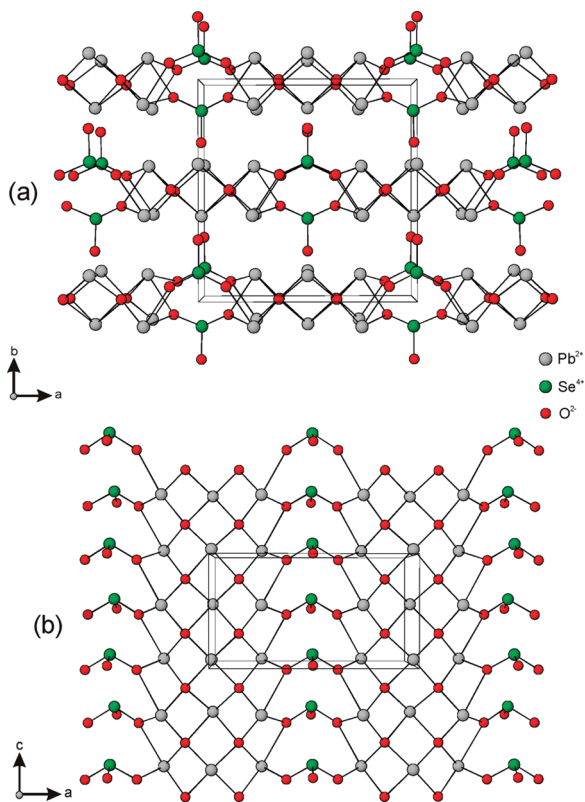
**Polarization Measurements.** The pellet used in the piezoelectric measurements was used in the polarization measurements. The polarization was measured on a Radiant Technologies RT66A Ferroelectric Test System with a TREK high voltage amplifier between room temperature and 165 °C in Delta 9023 environmental test chamber. The unclamped pyroelectric coefficient, defined as d*P*/d*T* (change in the polarization with respect to the change in temperature), was determined by measuring the polarization as a function of temperature. A detailed description of the methodology used has been published elsewhere.<sup>57</sup> To determine the ferroelectric behavior, the polarization loop was measured at room temperature under a static electric field of 13–30 kV/cm in the 5–200 Hz frequency range. For the pyroelectric measurements, the polarization was measured statically from room temperature to 165 °C in 20 °C increments, with an electric field of 30 kV/cm. The temperature was allowed to stabilize before the polarization was measured.

**Electronic Structure Calculations.** First principle electronic band structure calculations were performed with the plane wave pseudopotential<sup>58</sup> and tight-binding linear muffin-tin orbital (TB-LMTO)<sup>59,60</sup> methods based upon density functional theory (DFT).<sup>61,62</sup>

- (49) Sheldrick, G. M. *SHELXL-97 - A program for crystal structure refinement*; University of Goettingen: Goettingen, 1997.  
 (50) Spek, A. L. *PLATON*; Utrecht University: Utrecht, The Netherlands, 2001.  
 (51) Adams, D. M.; Stevens, D. C. *J. Chem. Soc., Dalton Trans.* **1977**, 1096.  
 (52) Gospodinov, G. G.; Sukova, L. M.; Petrov, K. I. *Zh. Neorg. Khim.* **1988**, 33, 1970.  
 (53) Sammes, N. M.; Tompsett, G.; Cartner, A. M. *J. Mater. Sci.* **1995**, 30, 4299.

- (54) Kubelka, P.; Munk, F. Z. *Tech. Phys.* **1931**, 12, 593.  
 (55) Tauc, J. *Mater. Res. Bull.* **1970**, 5, 721.  
 (56) Kurtz, S. K.; Perry, T. T. *J. Appl. Phys.* **1968**, 39, 3798.  
 (57) Ok, K. M.; Chi, E. O.; Halasyamani, P. S. *Chem. Soc. Rev.* **2006**, 35, 710.  
 (58) Pickett, W. E. *Comput. Phys. Rep.* **1989**, 9, 115.  
 (59) Tank, R. W. J. O.; Burckhardt, A.; Andersen, O. K. *TB-LMTO-ASA program*, Version 4.7c; Max-Planck Institute für Festkörperforschung: Stuttgart, Germany, 1994.  
 (60) Andersen, O. K. *Phys. Rev. B* **1975**, 12, 3060.  
 (61) Hohenberg, P.; Kohn, W. *Phys. Rev.* **1964**, 136, B864.  
 (62) Kohn, W.; Sham, L. J. *J. Phys. Rev.* **1965**, 140, A1133.





**Figure 1.** Ball-and-stick representations of the  $\text{Pb}_3\text{SeO}_5$  crystal structure in the  $ab$ -plane (a) and  $ac$ -plane (b). Note in part b that the polar  $\text{SeO}_3$  polyhedra are aligned.

As implemented in the Quantum ESPRESSO (4.0.3 version) package,<sup>63</sup> we initially utilized ultrasoft pseudopotentials (USPPs)<sup>64</sup> for all the elements to perform structural optimization with the generalized gradient approximation (GGA)<sup>65</sup> for the exchange-correlation corrections. All ions were relaxed until the Hellmann–Feynman force,<sup>66</sup> and the total energy changes were less than  $10^{-3}$  Rydberg (Ry) per atomic unit (a.u.) and  $10^{-4}$  Ry, respectively, between two consecutive self-consistent field steps. During the relaxations, the experimental symmetry of the structure was retained. A plane wave energy cutoff was set to 37 Ry. A Gaussian smearing of 0.01 Ry for Brillouin zone integrations was adopted with a  $4 \times 4 \times 6$   $k$ -point mesh in the C-centered orthorhombic unit cell. The relaxed structure was adopted in the TB-LMTO calculations within the atomic sphere approximation (ASA). The von Barth–Hedin local exchange-correlation potential was used for the local density approximation (LDA).<sup>67</sup> The radial scalar relativistic Dirac equation was solved for obtaining the partial waves. A total of 9 empty spheres were necessary to achieve space filling for  $\text{Pb}_3\text{SeO}_5$ . A total of 168 irreducible  $k$ -points from  $8 \times 8 \times 8$  grid was used for Brillouin zone integrations by the tetrahedron method.<sup>68,69</sup> The basis set consisted of Pb-6s/6p/[5d]/[5f], Se-4s/4p/[4d] and O-2s/2p orbitals where the orbi-

tal in bracket was treated with the downfolding technique.<sup>70</sup> Total energy changes of less than  $10^{-5}$  Ry indicated self-consistency.

## Results and Discussion

**Crystal Structure Description.** As the structure of  $\text{Pb}_3\text{SeO}_5$  has already been reported, only a brief description will be given here.  $\text{Pb}_3\text{SeO}_5$  exhibits a two-dimensional layered crystal structure, consisting of linked  $\text{PbO}_4$  and  $\text{SeO}_3$  polyhedra (see Figure 1a). The layers consist of “trimer slabs” of  $\alpha$ - $\text{PbO}$ -like  $\text{PbO}_4$  polyhedra that are connected by  $\text{SeO}_3$  groups (see Figure 1b). As we will discuss later, understanding the structural relationships between the reported material and  $\alpha$ - $\text{PbO}$  are critical to understanding the macroscopic polarity in  $\text{Pb}_3\text{SeO}_5$ . The trimer slabs consist of edge-shared  $\text{PbO}_4$  polyhedra that are linked along the  $a$ - and  $c$ -axes. The bridging  $\text{SeO}_3$  polyhedra are aligned in a parallel manner along the  $c$ -axis. Both unique  $\text{Pb}^{2+}$  cations are bonded to four oxygen atoms with Pb–O distances ranging from 2.194(10) to 2.727(5) Å, whereas the  $\text{Se}^{4+}$  cations is bonded to three oxygen atoms with Se–O distances ranging from 1.681(9) to 1.703(6) Å. In connectivity terms, the structure may be written as  $\{[\text{Pb}(1)\text{O}_{4/4}]^0 2[\text{Pb}(2)\text{O}_{2/4}\text{O}_{2/3}]^{-1/3} [\text{SeO}_{1/1}\text{O}_{2/3}]^{+2/3}\}^0$ . The local coordination of both  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$  are highly asymmetric attributable to their stereoactive lone-pair (see Figure 2). More details regarding the lone-pair will be given in the Electronic Structure Analysis section.

One of the most interesting features of  $\text{Pb}_3\text{SeO}_5$  is its structural relationship to  $\alpha$ - $\text{PbO}$ .  $\alpha$ - $\text{PbO}$  is a layered material consisting of edge-shared and puckered  $\text{PbO}_4$  polyhedra.<sup>71</sup> The  $\text{Pb}^{2+}$  cations exhibit a stereoactive lone-pair rendering each  $\text{PbO}_4$  polyhedron polar. Within each layer the  $\text{Pb}^{2+}$  polarization alternates direction, between “up” and “down”, resulting in a nonpolar centrosymmetric structure. This is exactly what is observed in the  $\alpha$ - $\text{PbO}$  section of  $\text{Pb}_3\text{SeO}_5$ . In  $\text{Pb}_3\text{SeO}_5$ , the  $\alpha$ - $\text{PbO}$  slabs are also pseudocentrosymmetric and are found as trimers—effectively “ $\text{Pb}_3\text{O}_3$ ” ( $3 \times \alpha$ - $\text{PbO}$ ) units. These pseudocentrosymmetric “ $\text{Pb}_3\text{O}_3$  slabs” are connected by the polar  $\text{SeO}_3$  polyhedra (see Figure 3). In Figure 3, the bridging  $\text{SeO}_3$  polyhedra are surrounded by a dotted blue box. Thus,  $\text{Pb}_3\text{SeO}_5$  may be thought of being built-up as,  $\text{Pb}_3\text{O}_3$  ( $3 \times \alpha$ - $\text{PbO}$ ) +  $\text{SeO}_2 \rightarrow \text{Pb}_3\text{SeO}_5$ . The bridging  $\text{SeO}_3$  polyhedra are not only *locally* polar, but are also aligned in a parallel manner rendering  $\text{Pb}_3\text{SeO}_5$  *macroscopically* polar. The question remains, however, what factors lead to the  $\text{SeO}_3$  polyhedra aligning in a parallel manner. To address this question, we used DFT calculations on a variety of hypothetical  $\text{Pb}_3\text{SeO}_5$  crystal structures, i.e., those where the  $\text{SeO}_3$  polyhedra are antiparallel (see the Electronic Structure Analysis section).

**Functional Properties.** We investigated the SHG, piezoelectric, and polarization properties of  $\text{Pb}_3\text{SeO}_5$ . Powder SHG measurements on sieved  $\text{Pb}_3\text{SeO}_5$  revealed an

(63) Baroni, S.; DalCorso, A.; de Gironcoli, S.; Giannozzi, P.; Cavazzoni, C.; Ballabio, G.; Scandolo, S.; Chiarotti, G.; Focher, P.; Pasquarello, A.; Laasonen, K.; Trave, A.; Car, R.; Marzari, N.; Kokalj, A. <http://www.quantum-espresso.org/> (accessed October 7, 2009).

(64) Vanderbilt, D. *Phys. Rev. B* **1990**, *41*, 7892.

(65) Perdew, J. P.; Burke, K.; Ernzerhof, M. *Phys. Rev. Lett.* **1996**, *77*, 3865.

(66) Bendt, P.; Zunger, A. *Phys. Rev. Lett.* **1983**, *50*, 1684.

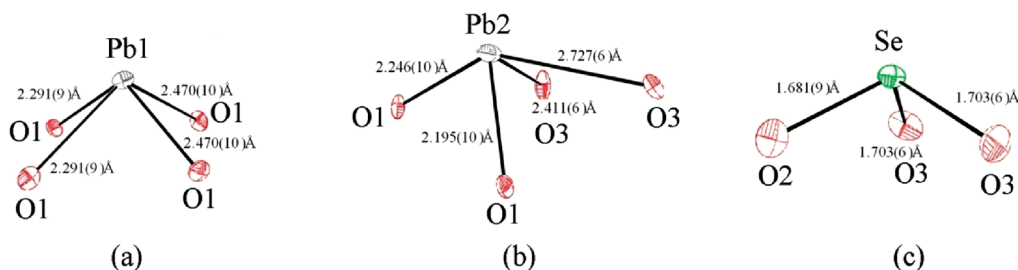
(67) Von Barth, U.; Hedin, L. *J. Phys. C: Solid State Phys.* **1972**, *5*, 1629.

(68) Jepsen, O.; Andersen, O. K. *Solid State Commun.* **1971**, *9*, 1763.

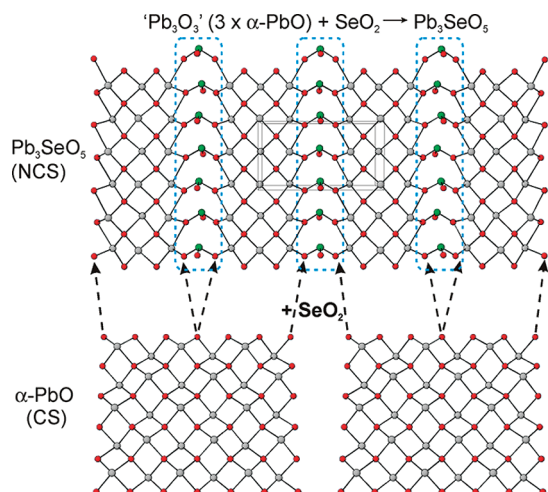
(69) Jepsen, O.; Andersen, O. K. *Phys. Rev. B* **1984**, *29*, 5965.

(70) Lambrecht, W. R. L.; Andersen, O. K. *Phys. Rev. B* **1986**, *34*, 2439.

(71) Dickinson, R. G.; Friauf, J. B. *J. Am. Chem. Soc.* **1924**, *46*, 2457.



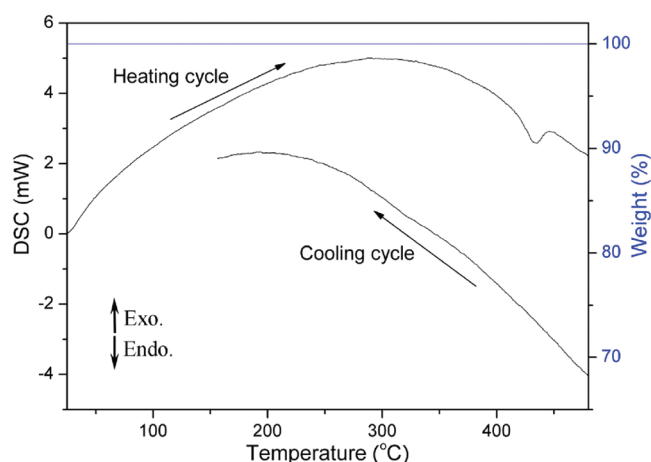
**Figure 2.** ORTEP diagrams (50% probability ellipsoids) for the (a) Pb(1)O<sub>4</sub>, (b) Pb(2)O<sub>4</sub>, and (c) SeO<sub>3</sub> polyhedra. Bond lengths are given next to each metal–oxygen bond.



**Figure 3.** Ball-and-stick representations of a layer of noncentrosymmetric Pb<sub>3</sub>SeO<sub>5</sub> (top) and centrosymmetric α-PbO (bottom) are shown. Pb<sub>3</sub>SeO<sub>5</sub> may be thought of as pseudocentrosymmetric trimer α-PbO slabs connected by SeO<sub>3</sub> polyhedra (blue box). Note that it is the alignment of the SeO<sub>3</sub> polyhedra that renders Pb<sub>3</sub>SeO<sub>5</sub> macroscopically polar.

efficiency of  $\sim 300 \times \alpha\text{-SiO}_2$  in the 45–63 mm particle size range. This efficiency is comparable to BaTiO<sub>3</sub> ( $400 \times \alpha\text{-SiO}_2$ ) and LiNbO<sub>3</sub> ( $600 \times \alpha\text{-SiO}_2$ ).<sup>56</sup>

Additional SHG measurements indicate Pb<sub>3</sub>SeO<sub>5</sub> is type 1 phase-matchable (see Figure S5 in the Supporting Information), with a  $\langle d_{\text{eff}} \rangle$  of  $\sim 22$  pm/V. Converse piezoelectric measurements were also performed and revealed a  $d_{33}$  value of  $\sim 81$  pm/V (see Figure S6 in the Supporting Information). The charge constant compares well to other selenites, such as LiH<sub>3</sub>(SeO<sub>3</sub>)<sub>2</sub> ( $d_{33} = 46$  pC/N).<sup>72</sup> Thus Pb<sub>3</sub>SeO<sub>5</sub> represents a rare example of a piezoelectric selenite. As Pb<sub>3</sub>SeO<sub>5</sub> is polar, ferroelectric and pyroelectric measurements were performed. Although ferroelectric-like polarization loops were observed (see Figure S7 in the Supporting Information), and their polarization magnitudes were frequency dependent, Pb<sub>3</sub>SeO<sub>5</sub> is *not* ferroelectric. The observed loops are attributable to dielectric loss, and not polarization reversal.<sup>73,74</sup> This indicates that the macroscopic polarization in Pb<sub>3</sub>SeO<sub>5</sub> cannot be “flipped” in the presence of an external electric field. Macroscopic polarization irreversibility implies



**Figure 4.** Thermogravimetric (TG) and differential scanning calorimetry (DSC) data for Pb<sub>3</sub>SeO<sub>5</sub>. The TG data (blue solid line) shows no weight loss up to  $\sim 650$  °C. In the DSC data (black solid line), an irreversible endothermic peak during the heating cycle at  $\sim 440$  °C is observed.

microscopic polarization irreversibility, thus it is relevant to examine the local polarization associated with the PbO<sub>4</sub> and SeO<sub>3</sub> polyhedra. As noted earlier and seen in Figure 3, the PbO<sub>4</sub> polyhedral polarizations are pointed in opposite directions. Thus, all of the polarization associated with Pb<sup>2+</sup> cancels. This is not the situation with the SeO<sub>3</sub> polyhedra. Also, as seen in Figure 3, the SeO<sub>3</sub> polyhedral polarizations are aligned in a parallel manner. If polarization reversal was to occur in Pb<sub>3</sub>SeO<sub>5</sub>, the polarization associated with the SeO<sub>3</sub> polyhedra would have to be reversed. As we will discuss in the Electronic Structure Analysis section, the SeO<sub>3</sub> polarization reversal is energetically very unfavorable. Pyroelectric measurements revealed a pyroelectric coefficient of  $-42 \mu\text{C}/(\text{m}^2 \text{ K})$  at 65 °C (see Figure S8 in the Supporting Information). The value is consistent with polar materials that are not ferroelectric, such as ZnO ( $-9.4 \mu\text{C}/(\text{m}^2 \text{ K})$ ), tourmaline ( $-4.0 \mu\text{C}/(\text{m}^2 \text{ K})$ ), and Li<sub>2</sub>Ti(IO<sub>3</sub>)<sub>6</sub> ( $-2.4 \mu\text{C}/(\text{m}^2 \text{ K})$ ).<sup>5,75</sup>

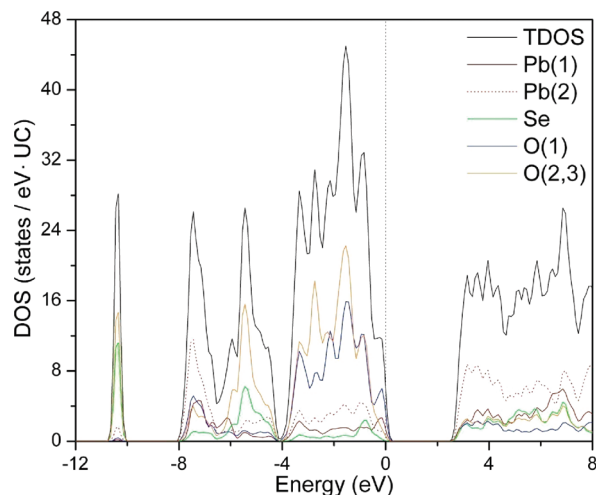
**Thermal Studies.** The thermal stability of Pb<sub>3</sub>SeO<sub>5</sub> was investigated through thermogravimetric (TGA) and differential scanning calorimetry (DSC). A phase transition or separation was observed initially when pellets of Pb<sub>3</sub>SeO<sub>5</sub> were sintered at 450 °C, as additional peaks were observed in the PXRD pattern (see Figure S1 in the Supporting Information). It should be noted that there

(72) Berlincourt, D.; Cook, W. R. Jr.; Rander, M. E. *Acta Crystallogr.* **1963**, *16*, 163.

(73) Scott, J. F. *J. Phys.: Condens. Matter* **2008**, *20*, 021001/1.

(74) Loidl, A.; Krohns, S.; Hemberger, J.; Lunkenheimer, P. *J. Phys.: Condens. Matter* **2008**, *20*, 191001/1.

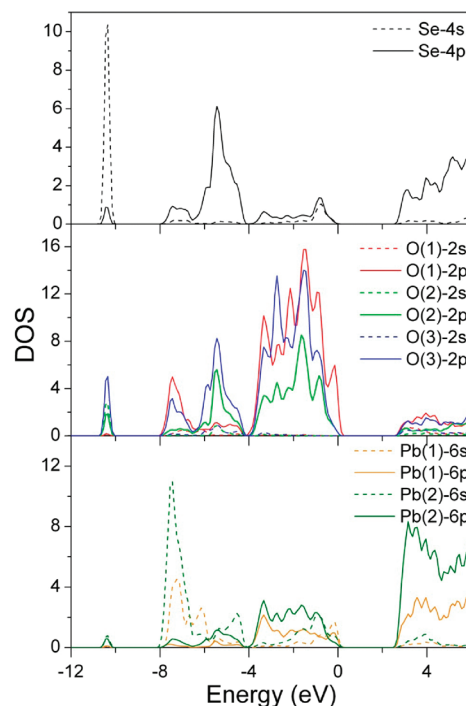
(75) Chang, H.-Y.; Kim, S.-H.; Halasyamani, P. S.; Ok, K. M. *J. Am. Chem. Soc.* **2009**, *131*, 2426.



**Figure 5.** TDOS and PDOSs of  $\text{Pb}_3\text{SeO}_5$  from the ultrasoft pseudopotential calculations. The vertical dotted line at 0 eV indicates the Fermi level: (black solid line) TDOS; (brown solid line) Pb(1) PDOS; (brown dotted line) Pb(2) PDOS; (green) Se PDOS; (blue) O(1) PDOS; (orange) O(2,3) PDOS.

was no color change in the sample. The TGA data indicated  $\text{Pb}_3\text{SeO}_5$  is stable to  $\sim 600^\circ\text{C}$ , after which the material rapidly loses  $\text{SeO}_2$  and  $\text{PbO}$  (see Figure S2 in the Supporting Information). DSC measurements revealed an irreversible endothermic peak at  $\sim 440^\circ\text{C}$  in the heating cycle (see Figure 4). As seen in Figure 4, this peak is not observed in the cooling cycle. Powder XRD measurements revealed additional peaks, and SHG measurements indicated the material was no longer SHG active. We are currently investigating the identity of this phase.

**Electronic Structure Analysis.** The electronic band structure of  $\text{Pb}_3\text{SeO}_5$  was performed using ultrasoft pseudopotential calculations. For the calculations, we used the relaxed structure self-consistently achieved as mentioned previously. The relaxed and experimental atomic positions and bond distances are in good agreement (see Table S1 in the Supporting Information). Figure 5 shows the total density of states (TDOS) and projected density of states (PDOSs) between  $-12$  and  $+6$  eV. An energy gap of  $\sim 2.75$  eV is calculated and confirms the insulating nature of the material. The calculated and experimentally determined energy gaps are in good agreement. Overall, a narrow and two broad bands are observed at  $\sim -10$  eV and from  $\sim -8$  eV to the Fermi level,  $E_F$ , respectively. The broad bands are separated by a narrow energy gap around  $-4$  eV. The two broad bands can be separated into upper,  $\sim 4$  eV to  $E_F$ , and lower,  $\sim -8$  to  $-4$  eV, bands. In order to resolve the individual atomic contributions, additional detailed PDOSs analyses were performed (see Figure 6) where the top, middle, and bottom panels reveal the Se-(4s,4p), O-(2s,2p), and Pb-(6s,6p) PDOSs. The narrow band at  $\sim -10$  eV is mainly composed of Se-4s and O(2,3)-2sp orbitals with a very small contribution from the Pb(2)-6sp orbitals. The broad bands mainly consist of Se-4p, O-2p, Pb-6s, and Pb-6p orbitals. The Se-PDOSs indicate that significant contribution of the Se-4p orbital appears in the top part of the lower band,  $\sim -6.5$  to  $\sim -4$  eV. In the Pb-PDOS,

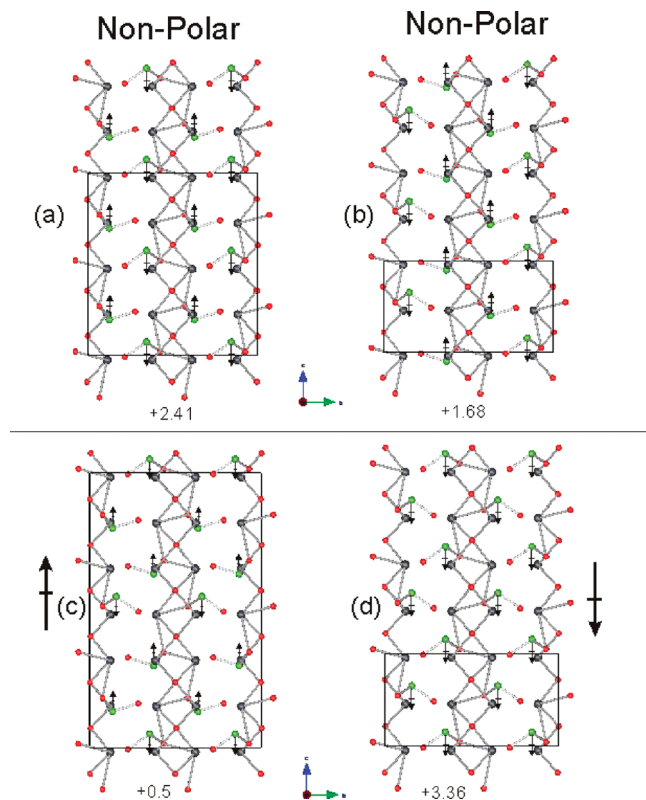


**Figure 6.** Detailed PDOSs of Se (top), O (middle), and Pb (bottom) from the ultrasoft pseudopotential calculations. The Fermi level is set to 0 eV.

larger and smaller Pb-6s orbital contributions appear in the lower band,  $\sim -8$  to  $\sim -4$  eV, and near the top part of the upper band,  $\sim -1$  eV to  $E_F$ , respectively. Conversely, larger and smaller Pb-6p contributions are observed in the upper,  $-4$  eV to  $E_F$ , and lower bands. Overall, the Pb(1) and Pb(2) PDOSs are similar to each other but the Pb(2)-6s orbital contribution is slightly shifted toward the lower energy region. In the O-PDOS, the O(1,3)-2p orbitals are dominant in the bottom part of the lower band,  $\sim -8$  to  $\sim 6.5$  eV, whereas the O(2,3)-2p orbitals are dominant at the top part of the lower band,  $\sim -6.5$  to  $\sim -4$  eV. Each of the O-2p orbitals contributes equally in the upper band,  $\sim -4$  to  $\sim -0.5$  eV, except for the top part of the upper band,  $\sim -0.5$  eV to  $E_F$ , which is mainly composed of contributions from the O(1)-2p orbital. These differences in the O- and Pb-PDOSs can be explained by the Se–O and Pb–O bonds (see Table 3), since these bonds influence their relative O-2p and Pb-6s orbital contributions. The contribution of the O(1)-PDOS is very small in the narrow band,  $\sim -10$  eV, and in the top part of the lower band,  $\sim -6.5$  to  $-4$  eV, since O(1) is not bonded to  $\text{Se}^{4+}$ . O(1) is bonded to both Pb(1) and Pb(2) and forms the shorter bond with Pb(2). As a result, the O(1)-2p PDOS is dominant in the vicinity of  $E_F$ , and the Pb(2)-6s PDOS is slightly shifted to lower energies. O(2) makes very long contacts with both Pb cations, thus the contribution of the O(2)-2p PDOS is negligible in the bottom part of the lower band. O(3) links Se with Pb(2), thus the O(3)-2p orbital contribution is significant in all the bands below  $E_F$ .

We also examined the bonding character of the bands through crystal orbital Hamilton population (COHP)

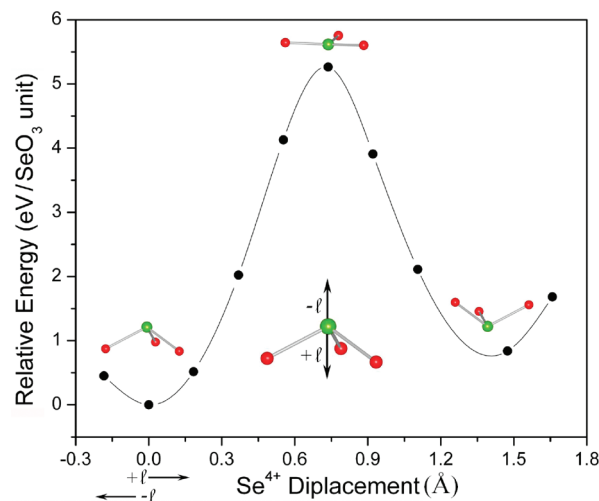




**Figure 7.** Ball-and-stick representations of four hypothetical  $\text{Pb}_3\text{SeO}_5$  structures in the  $bc$ -plane with differently aligned  $\text{SeO}_3$  polyhedra. The a and b structures are nonpolar and centrosymmetric, whereas c and d are polar. The macroscopic polarization direction is given in parts c and d. The unit cells are doubled and tripled in parts a and c, respectively. The relative energies, in electronvolts per unit cell, of the hypothetical structures compared to the experimental structure are given at the bottom of each part of the figure.

analyses.<sup>76</sup> The  $-\text{COHPs}$  for the  $\text{Se}-\text{O}$  and  $\text{Pb}-\text{O}$  ( $< 3.0 \text{ \AA}$ ) were carried out using TB-LMTO-ASA methods. These calculations also provided qualitatively equivalent TDOS and PDOSs in comparison to those calculated by the pseudopotential method. The  $-\text{COHP}$  curve for the  $\text{Se}-\text{O}$  shows that the bands above (below)  $\sim -3 \text{ eV}$  to  $E_F$  contain nonbonding (bonding) characters of the  $\text{Se}-\text{O}(2,3)$  bonds (see Figure S9 in the Supporting Information) attributable to strong  $sp$ -mixing of the Se orbitals. Overall, the  $-\text{COHP}$  for the  $\text{Pb}-\text{O}$  bonds is similar to  $\text{Pb}-\text{O}$  in  $\alpha\text{-PbO}$ , where a lone-pair is observed.<sup>77</sup> Similarly, we expect lone-pair formation on the  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$  cations (see the Direct Space Analysis section).

In order to investigate the parallel alignment of the  $\text{SeO}_3$  polyhedra, we created four hypothetical  $\text{Pb}_3\text{SeO}_5$  structures wherein the  $\text{PbO}$  framework is constant, but the alignment of the  $\text{SeO}_3$  polyhedra vary (see Figure 7). Recall that  $\text{Pb}_3\text{SeO}_5$  is macroscopically polar which is attributable to the parallel alignment of the locally polar  $\text{SeO}_3$  polyhedra. In Figure 7, ball-and-stick presentations of four hypothetical  $\text{Pb}_3\text{SeO}_5$  structures are shown. In all of the hypothetical structures, the local coordination of  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$  is the same as in the experimentally determined  $\text{Pb}_3\text{SeO}_5$  structure. The total energy for each



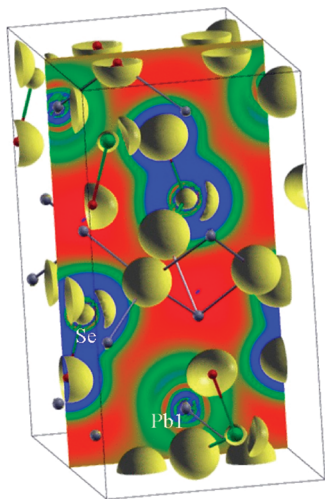
**Figure 8.** Energy landscape with respect to the  $\text{Se}^{4+}$  displacement for the inversion of the  $\text{SeO}_3$  polyhedra. The calculations (●) were performed, as described in the text, with the  $\text{Se}^{4+}$  cation moving in the  $+/-$  direction. The energy barrier to inversion is  $\sim 5.3 \text{ eV}$ .

structure was calculated using the ultrasoft pseudopotential method described earlier. With the hypothetical structures, two are nonpolar (Figure 7a and b) and two are polar (Figure 7c and d). In fact the structure shown in Figure 7d has all the  $\text{SeO}_3$  polyhedra inverted relative to the experimentally determined structure. In addition, the unit cells in the structures shown in Figure 7a and c are doubled and tripled respectively to accommodate the  $\text{SeO}_3$  inversion scheme. The relative energies of the hypothetical structures compared to the experimental structure are also given in Figure 7. As seen all of the hypothetical structures are energetically less stable than the experimentally determined  $\text{Pb}_3\text{SeO}_5$ . Interestingly, this instability increases proportional to the number of  $\text{SeO}_3$  polyhedra that are inverted, i.e., the most unstable structure in Figure 7d has all of the  $\text{SeO}_3$  polyhedra inverted. By inverting the  $\text{SeO}_3$  polyhedra, the distance between the  $\text{Se}^{4+}$  and  $\text{Pb}^{2+}$  cations are decreased, increasing the energetically unfavorable  $\text{Se}^{4+}$  lone-pair– $\text{Pb}^{2+}$  lone-pair interactions. Although additional hypothetical structures can be envisioned, we anticipate that any structures with inverted  $\text{SeO}_3$  polyhedra would be energetically unstable attributed to these lone-pair–lone-pair interactions.

It is also important to investigate and understand why  $\text{Pb}_3\text{SeO}_5$  although polar, is not ferroelectric, i.e., the macroscopic polarization is not reversible. Since the  $\text{PbO}$  framework in  $\text{Pb}_3\text{SeO}_5$  is pseudocentrosymmetric—all of the  $\text{PbO}_4$  dipole moments point in equal and opposite directions—any possible polarization reversal may be attributed solely to the  $\text{SeO}_3$  polyhedra. There are two polarization reversal “mechanisms” that do not involve breaking  $\text{Se}-\text{O}$  bonds. One is similar to the  $\text{NO}_2$  group in ferroelectric  $\text{NaNO}_2$ .<sup>78</sup> In this mechanism, the  $\text{SeO}_3$  group rotates parallel to the base of the polyhedron. Such a rotation would involve large movements of not

(77) Raulot, J.-M.; Baldinozzi, G.; Seshadri, R.; Cortona, P. *Solid State Sci.* **2002**, *4*, 467.

(78) Sawada, S.; Nomura, S.; Fujii, S. i.; Yoshida, I. *Phys. Rev. Lett.* **1958**, *1*, 320.



**Figure 9.** Electron density (ED) isosurface (yellow) at  $1 \text{ e}^-/\text{\AA}^3$  and contour map of (100) plane with RGB basis between 0 (red) and  $0.375 \text{ e}^-/\text{\AA}^3$  (blue).<sup>78</sup> The stereoactive lone-pairs on the  $\text{Se}^{4+}$  and  $\text{Pb}^{2+}$  are clearly observed. The plot was calculated using the TB-LMTO-ASA method.

only the oxide ligands, but also the lone-pair, and is thus considered highly unlikely. The second mechanism is an umbrella-type inversion of the  $\text{SeO}_3$  polyhedron—similar to  $\text{NH}_3$ . We performed frozen phonon calculations in order to evaluate how the total energy would vary during the hypothetical umbrella-type inversion.<sup>28</sup> In these calculations, the  $\text{Se}^{4+}$  cation was displaced parallel to the pseudo-3-fold axis in the  $\text{SeO}_3$  polyhedron. Figure 8 reveals the energy landscape for the  $\text{SeO}_3$  polyhedron with respect to the  $\text{Se}^{4+}$  displacement. The movement of the  $\text{Se}^{4+}$  toward the base of the  $\text{SeO}_3$  polyhedron is  $+/-$ , whereas displacement in the opposite direction is  $-/+$ . Two energy minima and one maximum are observed. The two minima correspond to the relative energies of the experimental and inverted  $\text{SeO}_3$  polyhedra. The energy of the inverted  $\text{SeO}_3$  polyhedra is raised by  $\sim 0.8 \text{ eV}$  compared to the original attributable to energetically unfavorable interactions between the  $\text{Pb}^{2+}$  and  $\text{Se}^{4+}$  cations. In the inverted structure, these cations are closer to each other. The maximum corresponds to the energy barrier for inversion and is  $\sim 5.3 \text{ eV}$ —comparable to the  $\text{IO}_3$  inversion in  $\text{Li}_2\text{Ti}(\text{IO}_3)_6$ .<sup>28</sup> This energy barrier is substantially higher than those found in well-known ferroelectrics such as  $\text{BaTiO}_3$  ( $\sim 1.8 \times 10^{-2} \text{ eV}$ ) and  $\text{PbTiO}_3$  ( $\sim 2.0 \times 10^{-1} \text{ eV}$ ).<sup>79</sup> This clearly demonstrates why  $\text{Pb}_3\text{SeO}_5$  is not

ferroelectric, as the polarization reversal of the  $\text{SeO}_3$  polyhedra is energetically very unfavorable, i.e., nearly 500 and 45 times the energy required for  $\text{BaTiO}_3$  and  $\text{PbTiO}_3$ , respectively.

**Direct Space Analysis.** As described in the previous section, stereoactive lone-pairs are expected to occur on the  $\text{Se}^{4+}$  and  $\text{Pb}^{2+}$  cations. To visualize these lone-pairs, electron localization functions (ELFs) and electron density (ED) calculations were performed using the TB-LMTO-ASA method. Figure 9 gives a plot of the ED iso-surface and (100) contour map. The ED iso-surface plotted at  $1 \text{ e}^-/\text{\AA}^3$  and between 0 and  $0.375 \text{ e}^-/\text{\AA}^3$  clearly reveals highly asymmetric lobes on the  $\text{Se}^{4+}$  and  $\text{Pb}^{2+}$  cations, respectively. These asymmetric lobes may be thought of as stereoactive lone-pairs and are consistent with our ELF calculations where lobe-like iso-surfaces, with  $\eta = 0.85$ , are clearly observed near the cations (see Figure S10 in the Supporting Information). With the lone-pairs, we also consider any relevant lone-pair–lone-pair interactions. The  $\text{Se}^{4+}$  and  $\text{Pb}^{2+}(1)$  lone-pairs are perpendicular to each other and are at a distance of  $\sim 2.7 \text{ \AA}$ . Thus, a weak repulsive lone-pair–lone-pair interaction could be envisioned. We speculate that the irreversible structural change may be associated with this repulsion.

### Concluding Remarks

$\text{Pb}_3\text{SeO}_5$  is a novel NCS and polar material, whose macroscopic polarity is wholly attributable to the  $\text{SeO}_3$  polyhedra. Although macroscopically polar, the material is not ferroelectric, i.e., the polarization is not reversible. The material, however, does exhibit strong SHG, piezoelectric, and pyroelectric behavior. It is also of interest to note that  $\text{Pb}_3\text{SeO}_5$  undergoes an irreversible phase transition at  $\sim 440^\circ\text{C}$ , that we speculate is attributable to weak lone-pair–lone-pair repulsions. In order to gain a deeper insight into these repulsions, we are investigating materials that contain two lone-pair cations.<sup>80</sup>

**Acknowledgment.** We thank the Welch Foundation (Grant E-1457), NSF (DMR-0652150), and ACS PRF (47345-AC10) for support.

**Supporting Information Available:** Additional experimental and theoretical data. This material is available free of charge via the Internet at <http://pubs.acs.org>.

(79) Cohen, R. E. *Nature (London)* **1992**, 358, 136.

(80) Porter, Y.; Halasyamani, P. S. *Inorg. Chem.* **2003**, 42, 205.